

# A Second-Order Approach to Learning with Instance-Dependent Label Noise

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Paper & Code:



## Motivating Example

**Class-dependent** label noise (CDN):  $\forall X : \mathbb{P}(\tilde{Y}|Y^*, X) = \mathbb{P}(\tilde{Y}|Y^*)$ .

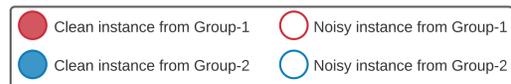
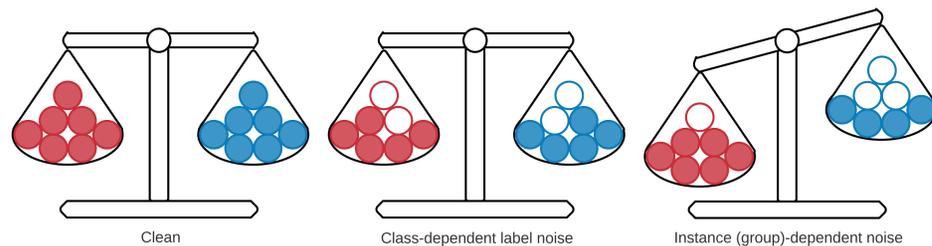
**Instance-dependent** label noise (IDN):  $\exists X : \mathbb{P}(\tilde{Y}|Y^*, X) \neq \mathbb{P}(\tilde{Y}|Y^*)$

**Example:**

Two groups of instances. Intra-group: CDN; Inter-group: IDN.

Empirical Risk Minimization (ERM) of instances from two groups:

$$\text{Loss} = \sum_{i \in \text{Group-1}} \text{Loss}_i + \sum_{j \in \text{Group-2}} \text{Loss}_j$$



**Intuition:** Compare the weights of group 1 with group 2, we find:

**Clean:** no noise  $\Rightarrow$

equal #instances contribute to clean loss  $\Rightarrow$  equal weights in ERM

**CDN:** equal noise  $\Rightarrow$

equal #instances contribute to clean loss  $\Rightarrow$  equal weights in ERM

**IDN:** Group 2: larger noise  $\Rightarrow$

less #instances contribute to clean loss  $\Rightarrow$  smaller weights in ERM

## Problems & Solutions (Overview)

**One-sentence summary:**

We use covariance to compensate for the “imbalances” caused by IDN such that the challenging IDN can be transformed to a easier CDN one.

**Problems:**

1. Label noise  $(X, \tilde{Y}) \rightarrow$  Wrong correlation patterns

2. Expensive human-efforts to reduce label noise

**Challenges:**

1. Unknown instance-dependent noise rates  $\mathbb{P}(\tilde{Y}|Y^*, X)$ , while most existing works [1-5] **assume feature independency**:  $\mathbb{P}(\tilde{Y}|Y^*, X) = \mathbb{P}(\tilde{Y}|Y^*)$

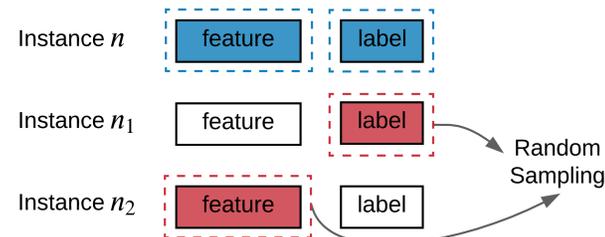
2. Loss-correction/reweighting [1-3]: **Hard to estimate**  $\mathbb{P}(\tilde{Y}|Y^*, X), \forall X$

3. IDN causes **imbalances** in different feature group (see Motivation)

**Solutions:** CAL: IDN  $\xrightarrow{\text{2nd-Order}}$  CDN  $\xrightarrow{\text{1st-Order}}$  Clean

## Peer Loss (Use First-Order Statistics)

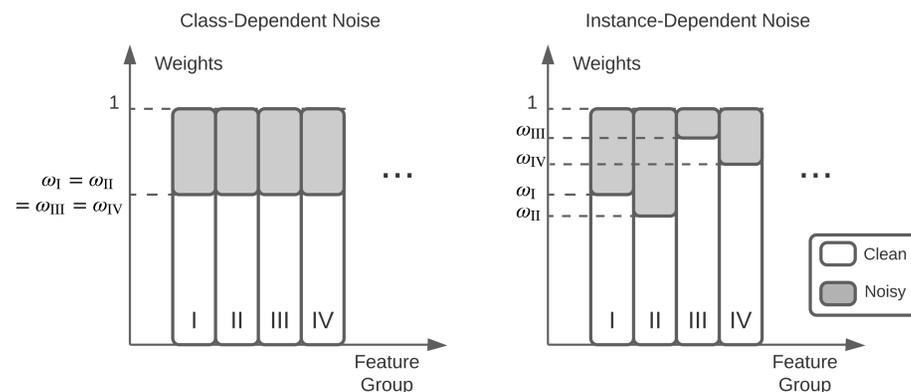
**Definition:**  $\ell_{\text{PL}}(f(x_n), \tilde{y}_n) := \ell(f(x_n), \tilde{y}_n) - \ell(f(x_{n_1}), \tilde{y}_{n_2})$



**Lemma:** Peer loss [4] is invariant to CDN: NoisyPL =  $\omega$  · CleanPL

**Summary:** 1) CDN  $\xrightarrow{\text{Peer Loss}}$  Clean; 2) Unknown  $\omega$ : Noise  $\uparrow$ , weight  $\omega \downarrow$

## Insufficiency of First-Order Statistics



**Summary:** IDN causes weights imbalances

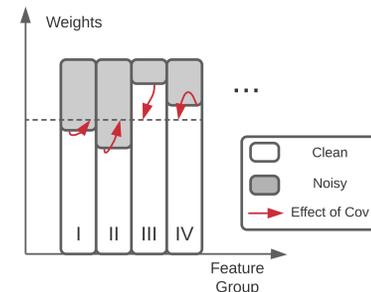
**CDN:** Only one unknown constant  $\omega$ . *Equal* for all features.

**IDN:** Multiple unknown constants  $\omega_g$ . *Down-weight* high-noise features.

## Covariance-Assisted Learning (CAL)

**Our method:** Peer Loss + Covariance (requires constructing  $\hat{D}$  for  $T$ ):

$$\ell_{\text{CAL}}(f(x_n), \tilde{y}_n) = \ell_{\text{PL}}(f(x_n), \tilde{y}_n) - \text{Cov}(\text{Noise Trans. } T, \text{Model Pred.})$$



**Summary:**

• CAL balances weights of each feature

– High-noise (I, II): improve weights

– Low-noise (III, IV): reduce weights

• IDN  $\xrightarrow{\text{Covariance}}$  CDN  $\xrightarrow{\text{Peer Loss}}$  Clean

**Benefits:** CAL is a “soft” correction (vs. “hard” label correction)

• Use an average term, less sensitive to estimation of each instance

• Tolerant of inaccurate  $\hat{D}$

**Algorithm (Sketch)**

1. Construct  $\hat{D}$  (unbiased estimate of  $D^* \sim \mathcal{D}^*$ ) with sample sieve [5]

2. Estimate (unbiased)  $\hat{T}$  with  $\hat{D}$  (complexity  $O(\text{SampleSize})$ )

3. [Train DNN] Implement CAL in SGD (each point  $O(1)$  complexity)

## Theoretical Guarantee

**Theorem:**

1) With perfect covariance estimates,  $\mathbb{1}_{\text{CAL}}$  is robust to IDN (induces the Bayes optimal classifier).

2) With imperfect covariance estimates, error rate can be upper bounded.

## Experiments

Table: Comparison of test accuracies (%) using different methods.

Method	Inst. CIFAR10			Inst. CIFAR100		
	$\eta = 0.2$	$\eta = 0.4$	$\eta = 0.6$	$\eta = 0.2$	$\eta = 0.4$	$\eta = 0.6$
CE (Standard)	85.45 $\pm$ 0.57	76.23 $\pm$ 1.54	59.75 $\pm$ 1.30	57.79 $\pm$ 1.25	41.15 $\pm$ 0.83	25.68 $\pm$ 1.55
Forward $T$ [2]	87.22 $\pm$ 1.60	79.37 $\pm$ 2.72	66.56 $\pm$ 4.90	58.19 $\pm$ 1.37	42.80 $\pm$ 1.01	27.91 $\pm$ 3.35
T-Revision [3]	90.04 $\pm$ 0.46	84.11 $\pm$ 2.47	72.18 $\pm$ 2.47	58.00 $\pm$ 0.36	43.83 $\pm$ 8.42	36.07 $\pm$ 9.73
Peer Loss [4]	89.12 $\pm$ 0.76	83.26 $\pm$ 0.42	74.53 $\pm$ 1.22	61.16 $\pm$ 0.64	47.23 $\pm$ 1.23	31.71 $\pm$ 2.06
CORES <sup>2</sup> [5]	91.14 $\pm$ 0.46	83.67 $\pm$ 1.29	77.68 $\pm$ 2.24	66.47 $\pm$ 0.45	58.99 $\pm$ 1.49	38.55 $\pm$ 3.25
CAL	<b>92.01<math>\pm</math>0.75</b>	<b>84.96<math>\pm</math>1.25</b>	<b>79.82<math>\pm</math>2.56</b>	<b>69.11<math>\pm</math>0.46</b>	<b>63.17<math>\pm</math>1.40</b>	<b>43.58<math>\pm</math>3.30</b>

## Relevant Works

[1] T. Liu & D. Tao. “Classification with noisy labels by importance reweighting.” *TPAMI'15*.

[2] G. Patrini, et al. “Making deep neural networks robust to label noise: A loss correction approach.” *CVPR'17*.

[3] X. Xia, et al. “Are anchor points really indispensable in label-noise learning?” *NeurIPS'19*.

[4] Y. Liu & H. Guo. “Peer loss functions: Learning from noisy labels without knowing noise.” *ICML'20*.

[5] H. Cheng, et al. “Learning with instance-dependent label noise: A sample sieve approach.” *ICLR'21*.

**Related other works from our lab**

• CE  $\rightarrow$  f-divergence: *When optimizing f-divergence is robust with label noise, ICLR'21*

• Estimate transition matrix with clusterability: *Clusterability as an Alternative to Anchor Points When Learning with Noisy Labels, ICML'21*

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